

Virtual Memory (Part I)

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Motivation and Background

Motivation

- ▶ A **program** needs to be in **memory** to execute.
- ▶ But, **entire program rarely used**.
 - Error code, unusual routines, large data structures
- ▶ Entire program code **not needed at same time**.

- ▶ Consider ability to execute **partially-loaded program**.

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 - **Increased CPU utilization** and **throughput** with no increase in response time or turnaround time.
- ▶ **Less I/O needed** to load or swap programs into memory: each user program runs **faster**.

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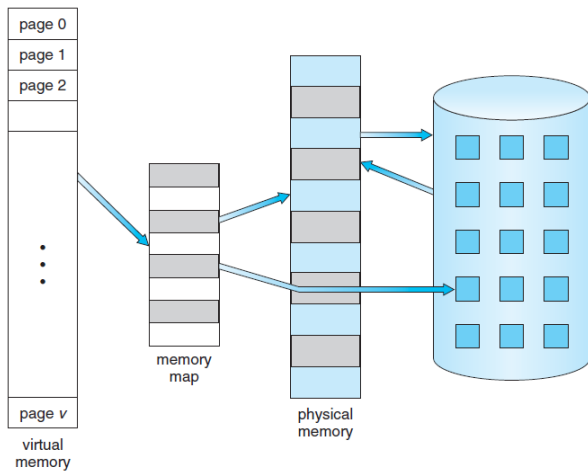
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- ▶ More programs running concurrently.

Virtual Memory (2/2)



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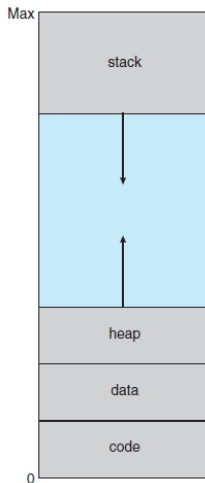
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- ▶ **MMU** must map logical to physical.

Virtual Address Space (2/3)



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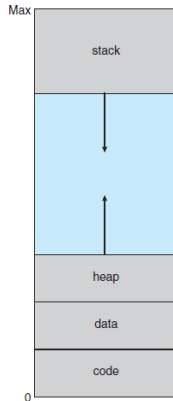
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- ▶ The **hole** between the heap and the stack is part of the **virtual address space**, but will require actual physical pages only if the heap or stack **grows**.
- ▶ Virtual address spaces that **include holes** are known as **sparse** address spaces.

Heap vs. Stack

► Stack

- Stores **local variables** created by functions.
- New variables are **pushed** onto the stack.
- When a function exits, all of its pushed variables are **freed**.



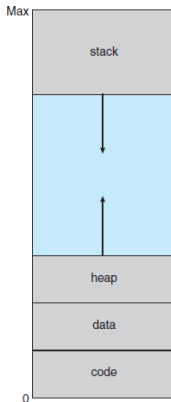
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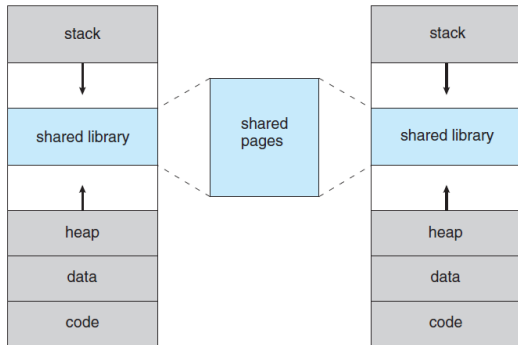
► Heap

- Used for **dynamic allocation**.
- Use `malloc()` or `calloc()` to allocate memory on the heap.
- Use `free()` to deallocate the memory.



Virtual Memory Benefits

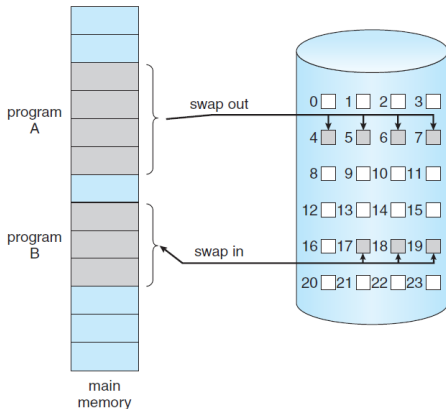
- ▶ Separating **logical memory** from **physical memory**.
- ▶ **Page sharing**.



Demand Paging

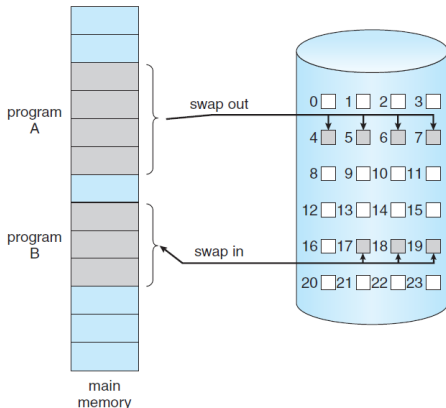
Demand Paging (1/2)

- ▶ Could bring **entire process** into memory at load time, or bring **a page into memory** only **when it is needed**.



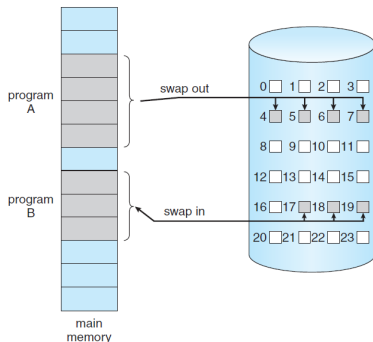
Demand Paging (1/2)

- ▶ Could bring **entire process** into memory at load time, or bring a **page into memory** only **when it is needed**.
- ▶ A **demand-paging** system is similar to a **paging system** with **swapping**.



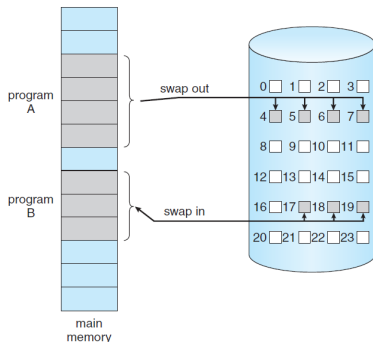
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- ▶ A **lazy swapper** never swaps a page into memory unless that page will be **needed**.



Demand Paging (2/2)

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- ▶ A **lazy swapper** never swaps a page into memory unless that page will be **needed**.
- ▶ A **swapper** that deals with pages is a **pager**.



Basic Concepts

- ▶ The **pager** guesses **which pages** will be used before swapping out again.

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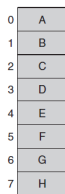
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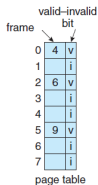
- ▶ The **pager** guesses **which pages** will be used before swapping out again.
- ▶ The pager brings only **the needed pages** into memory.
- ▶ Uses **valid-invalid bit** to **distinguish** between the pages that are in memory and the pages that are on the disk?

v: memory resident

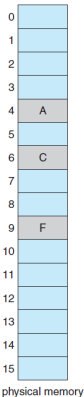
i: not in memory



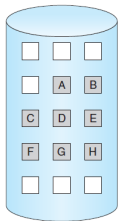
logical memory



page table



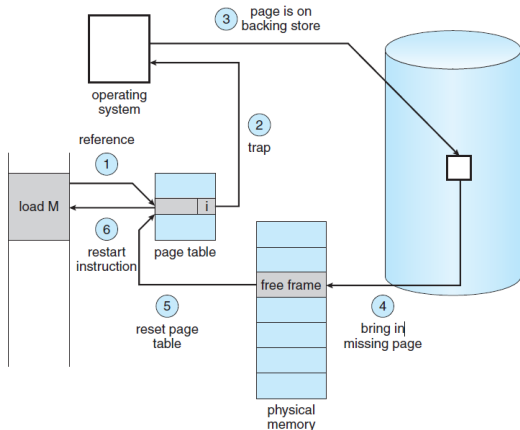
physical memory



- ▶ Access to a page marked **invalid** causes a **page fault**.
- ▶ Causing a trap to the OS: brings the **desired page into memory**.

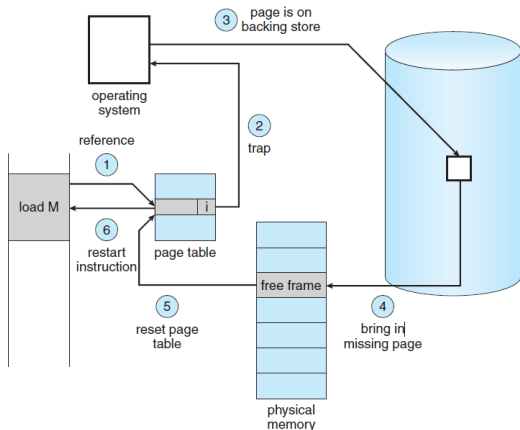
Handling Page Fault (1/6)

- ▶ Check an **internal table** for the process to determine whether the reference was a **valid** or an **invalid** memory access.



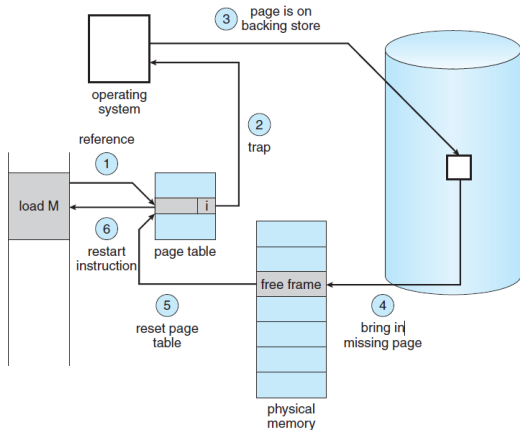
Handling Page Fault (2/6)

- ▶ If the reference was **invalid**, we **terminate** the process.
- ▶ If it was **valid** but we have not yet brought in that page, we now **page it in**.



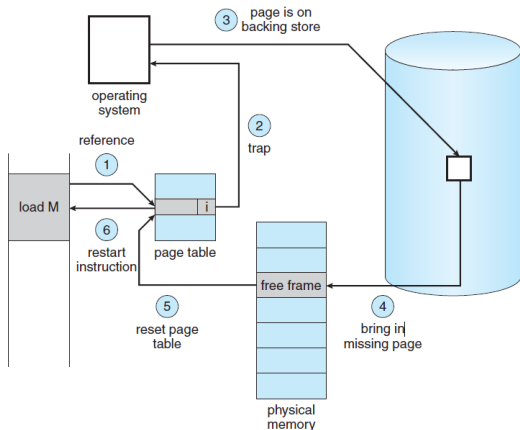
Handling Page Fault (3/6)

- ▶ We find a **free frame**.



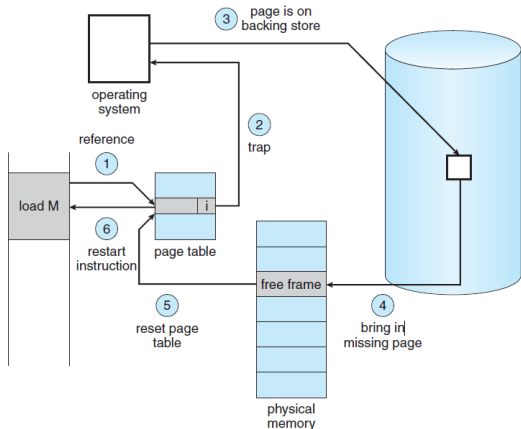
Handling Page Fault (4/6)

- ▶ We schedule a disk operation to **read the desired page** into the newly allocated frame.



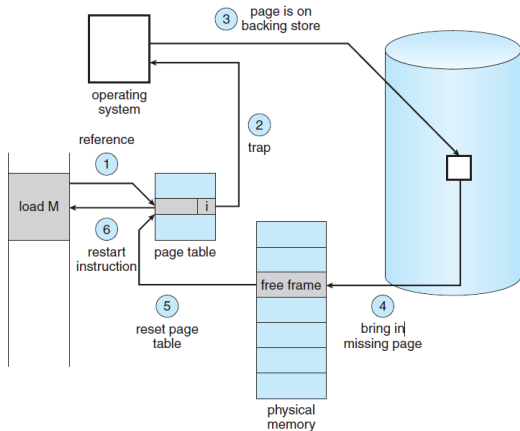
Handling Page Fault (5/6)

- ▶ When the disk read is complete, we **modify** the **internal table** kept with the process and the page table to indicate that the page is now in memory.



Handling Page Fault (6/6)

- ▶ We restart the instruction that was interrupted by the trap.



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- ▶ **Pure demand paging**

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- ▶ **Unacceptable system performance**
- ▶ **Locality of reference** results in reasonable performance from demand paging.

Demand Paging Hardware

- ▶ The **hardware** to support **demand paging** is the same as the hardware for **paging** and **swapping**:
 - **Page table** with valid-invalid bit
 - **Secondary memory** with **swap** space
- ▶ The ability to **restart any instruction** after a page fault.

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- ▶ 4. Check that the **page reference** was **legal** and determine the **location** of the page on the **disk**.

Stages in Demand Paging (2/3)

- ▶ 5. Issue a **read from the disk** to a **free frame**:
 - **Wait** in a **queue** for this device until the read request is serviced.
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- ▶ 7. Receive an **interrupt** from the disk I/O subsystem (**I/O completed**).

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- ▶ 12. **Restore** the user registers, process state, and new page table, and then resume the interrupted instruction.

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- ▶ Effective Access Time (EAT)
- ▶ $EAT = (1 - p) \times \text{memory_access} + p \times \text{page_fault_time}$

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- ▶ If $p = 0.001$, then $EAT = 8.2 \text{microseconds}$: this is a slowdown by a factor of 40.
- ▶ If want performance degradation < 10 percent:
 - $220 > 200 + p \times 7,999,800$
 - $20 > p \times 7,999,800$
 - $p < .0000025$: less than one page fault in every 400,000 memory accesses

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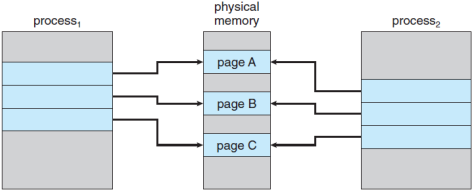
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- ▶ Copy entire process image to swap space at process load time.
 - Then page in and out of swap space.
- ▶ Demand page in from program binary on disk, but discard rather than paging out when freeing frame.
 - Pages not associated with a file, i.e., heap and stack (anonymous memory) still need to write to swap space.

Copy-on-Write

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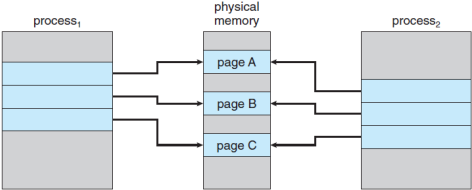
- ▶ **Copy-on-Write** allows both **parent** and **child** processes to initially share the same pages in memory.
- ▶ If either process **modifies a shared page**, only then is the page copied.

Copy-on-Write Example

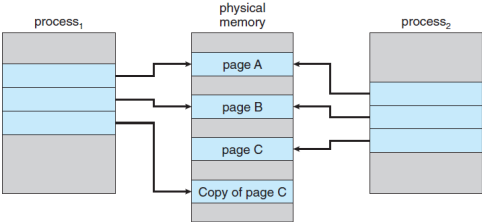


Before modification

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Before modification



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More About Copy-on-Write

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 - **Pool** should always have **free frames** for fast demand page execution.
 - **Zero-fill-on-demand** pages have been zeroed-out before being allocated, thus **erasing the previous contents**.
- ▶ **vfork()** variation on **fork()** does not use Copy-on-Write: with **vfork()**, the parent process is suspended, and the child process uses the address space of the parent.

Page Replacement

What Happens if There is no Free Frame?

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- ▶ And, we run **six processes**, each of which is **ten pages** in size, but actually uses only **five pages**.

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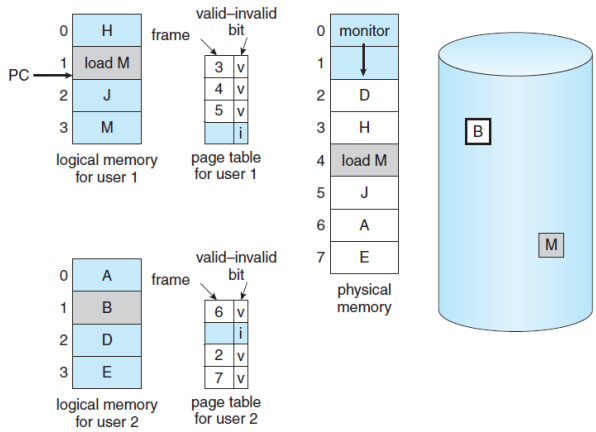
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- ▶ Increasing the degree of **multiprogramming**: **over-allocating memory**

Over-Allocation of Memory

- ▶ While a user process is **executing**, a **page fault** occurs.
- ▶ The OS determines where the **desired page** is residing on the **disk**.
- ▶ But, it finds that there are **no free frames** on the free-frame list.
- ▶ **Need for page replacement**

Need For Page Replacement



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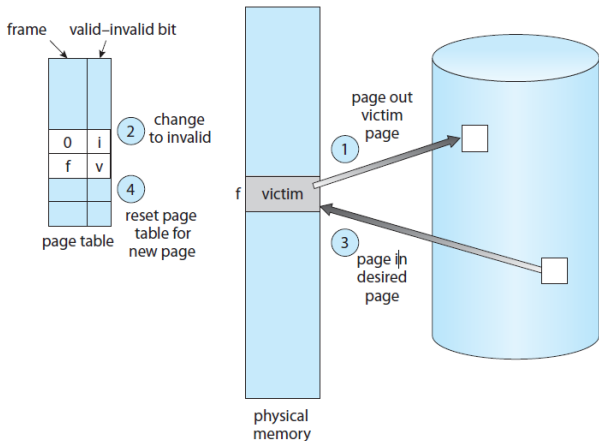
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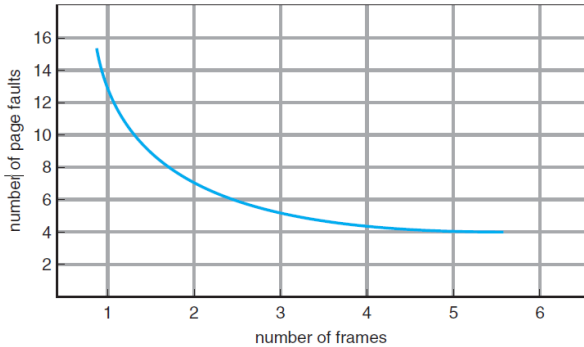
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- ③ Bring the desired page into the (newly) free frame; update the page and frame tables
- ④ Continue the process by restarting the instruction that caused the trap.

Page Replacement



- ▶ Use **modify (dirty) bit** to **reduce overhead** of page transfers - only **modified pages** are written to disk.

Page Faults vs. The Number of Frames



Evaluate Page Replacement Algorithms

- ▶ Evaluate algorithm by running it on a particular string of memory references (reference string) and computing the number of page faults on that string.
- ▶ String is just page numbers, not full addresses.
- ▶ For example, a reference string could be
7, 0, 1, 2, 0, 3, 0, 4, 2, 3, 0, 3, 0, 3, 2, 1, 2, 0, 1, 7, 0, 1

Page Replacement Algorithms

- ▶ First-In-First-Out (FIFO) page replacement
- ▶ Optimal page replacement
- ▶ Least Recently Used (LRU) page replacement
- ▶ LRU-Approximation page replacement
- ▶ Counting-Based page replacement

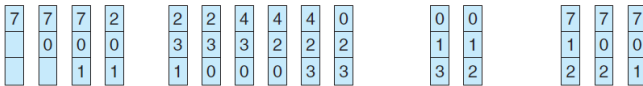
FIFO Page Replacement

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- ▶ Reference string: 7,0,1,2,0,3,0,4,2,3,0,3,2,1,2,0,1,7,0,1
- ▶ 3 frames (3 pages can be in memory at a time per process)

reference string

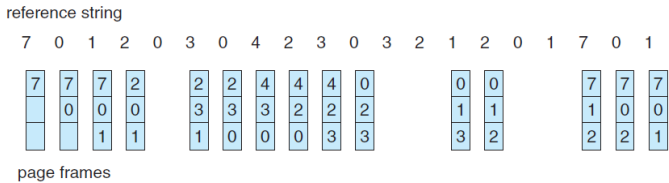
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page frames

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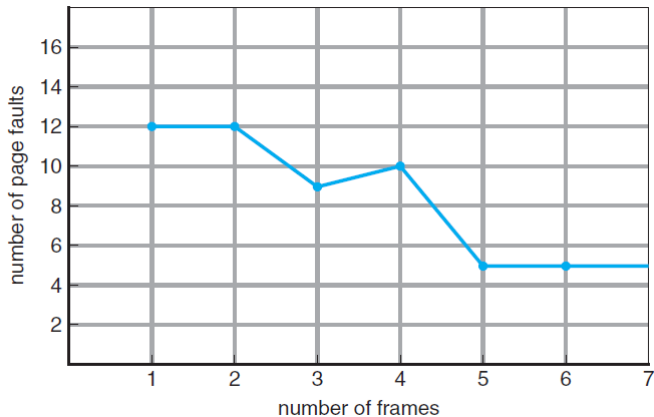
- ▶ Reference string: 7,0,1,2,0,3,0,4,2,3,0,3,2,1,2,0,1,7,0,1
- ▶ 3 frames (3 pages can be in memory at a time per process)



- ▶ 15 page faults

FIFO Belady's Anomaly

- ▶ Adding more frames can cause more page faults: **Belady's Anomaly**



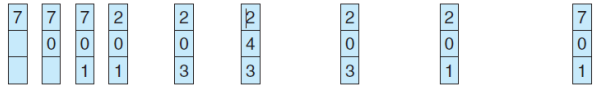
Optimal Page Replacement

Optimal Page Replacement

- ▶ Replace page that will not be used for **longest period of time**: 9 page fault is **optimal** for the example.
- ▶ How do you know this? Can't read the future

reference string

7 0 1 2 0 3 0 4 2 3 0 3 2 1 2 0 1 7 0 1



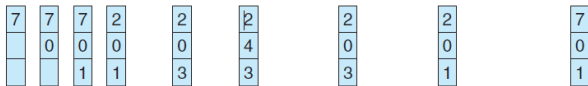
page frames

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page frames

- ▶ Used for measuring **how well your algorithm performs**.

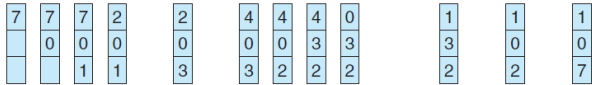
LRU Page Replacement

LRU Page Replacement

- ▶ Use **past knowledge** rather than the **future**.
- ▶ Replace page that has **not been used in the most amount of time**

reference string

7 0 1 2 0 3 0 4 2 3 0 3 2 1 2 0 1 7 0 1



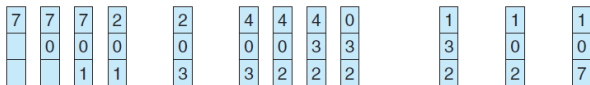
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page frames

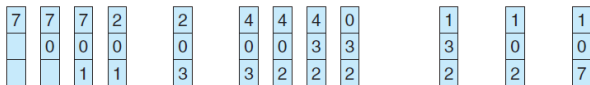
- ▶ **12 faults: better than FIFO but worse than OPT**

LRU Page Replacement

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reference string

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page frames

- ▶ **12 faults: better than FIFO but worse than OPT**
- ▶ Generally good algorithm and frequently used

LRU Implementation (1/2)

- ▶ Counter implementation
- ▶ Every page entry has a counter; every time page is referenced through this entry, copy the clock into the counter.
- ▶ When a page needs to be changed, look at the counters to find smallest value.
- ▶ Search through table needed.

LRU Implementation (2/2)

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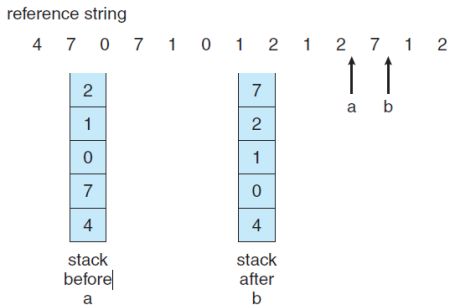
- ▶ Stack implementation
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- ▶ Stack implementation
- ▶ Keep a stack of page numbers in a double link form.
- ▶ Page referenced:
 - Move it to the top
 - Requires 6 pointers to be changed
- ▶ No search for replacement.
- ▶ LRU and OPT are cases of stack algorithms with no Belady's Anomaly.

Stack Implementation

- Use of a stack to record **most recent page references**.



LRU-Approximation Page Replacement

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- ▶ LRU needs **special hardware** and still **slow**
- ▶ Improvements: **LRU-Approximation**
 - Reference bit
 - Second-chance algorithm
 - Enhanced second-chance algorithm

- ▶ With each page associate a bit, initially = 0

Reference Bit

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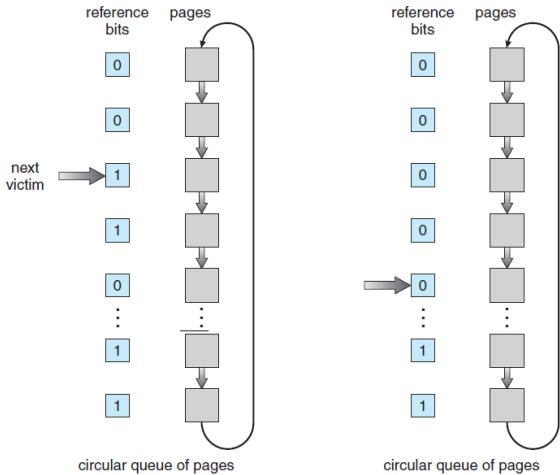
Reference Bit

- ▶ With each page associate a bit, initially = 0
- ▶ When page is referenced, bit set to 1
- ▶ Replace any with reference bit = 0 (if one exists)
- ▶ We do not know the order

Second-Chance Algorithm (1/2)

- ▶ It is also called **clock algorithm**.
- ▶ Generally **FIFO**, plus hardware-provided **reference bit**
- ▶ If page to be replaced has
 - Reference bit = 0 → **replace it**
 - Reference bit = 1 then, set reference bit 0, **leave page in memory**, and replace **next page**, subject to **same rules**.

Second-Chance Algorithm (2/2)



Enhanced Second-Chance Algorithm

- ▶ Improve algorithm by using **reference bit** and **modify bit** (**reference, modify**)

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 - ② $(0, 1)$ not recently used but modified: not quite as good, **must write out before replacement**
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- ▶ When page replacement called for, use the clock scheme but use the four classes replace page in lowest non-empty class
- ▶ Might need to search circular queue **several times**.

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- ▶ **Least Frequently Used (LFU)** algorithm: replaces page with **smallest count**.
- ▶ **Most Frequently Used (MFU)** algorithm: based on the argument that the page with the smallest count was **probably just brought in** and has yet to be used.

Summary

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- ▶ Virtual memory: much larger than physical memory
- ▶ Demand paging similar to paging + swapping
- ▶ Page fault
- ▶ Page replacement algorithms:
 - FIFO, optimal, LRU, LRU-approximate, counting-based

Questions?

Acknowledgements

Some slides were derived from Avi Silberschatz slides.